

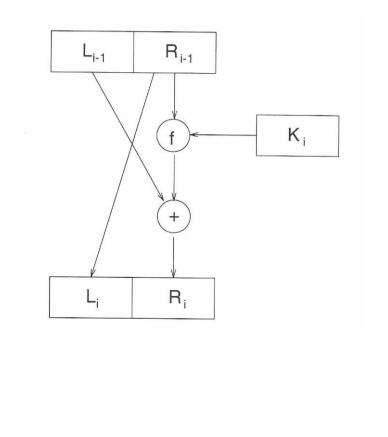
November 22, 2006

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#### **Feistel Networks**

- Encryption:
- Input:  $P = L_{i-1} | R_{i-1} . |L_{i-1}| = |R_{i-1}|$ -  $L_i = R_{i-1}$ 
  - $R_i = L_{i-1} \oplus F(K_i, R_{i-1})$
- Decryption?
- No matter which function is used as F, we obtain a permutation (i.e., F is reversible even if f is not).



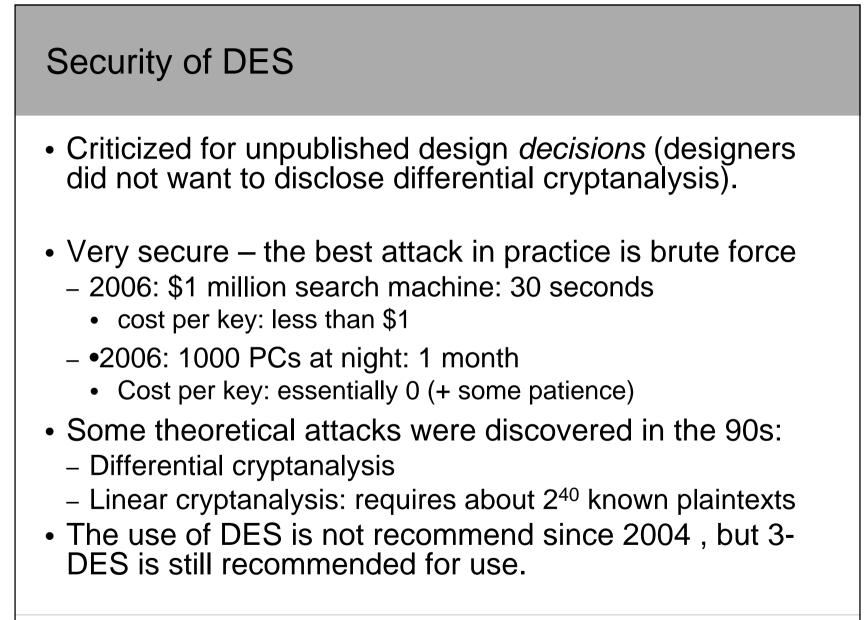
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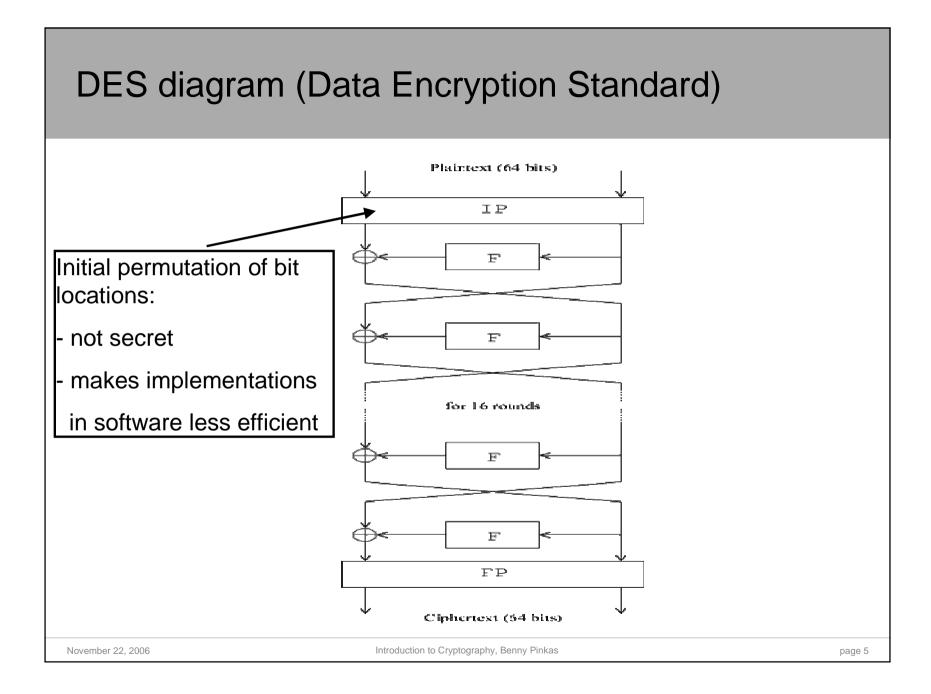
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# DES (Data Encryption Standard)

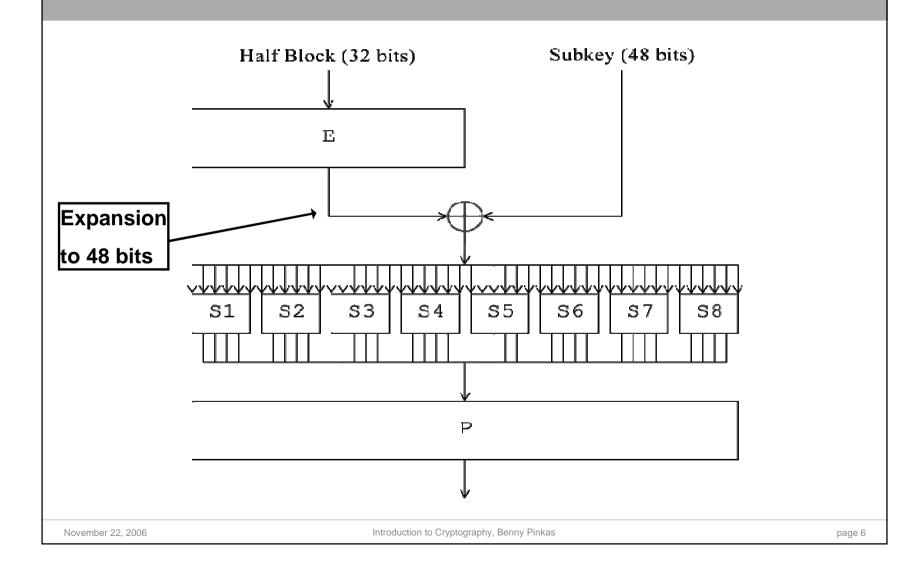
DES (Data Encryption Standard)

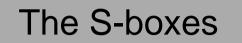
- Designed by IBM and the NSA, 1977.
- 64 bit input and output
- 56 bit key
- 16 round Feistel network
- Each round key is a 48 bit subset of the key
- Throughput ≈ software: 10Mb/sec, hardware: 1Gb/sec (in 1991!).





# **DES F functions**



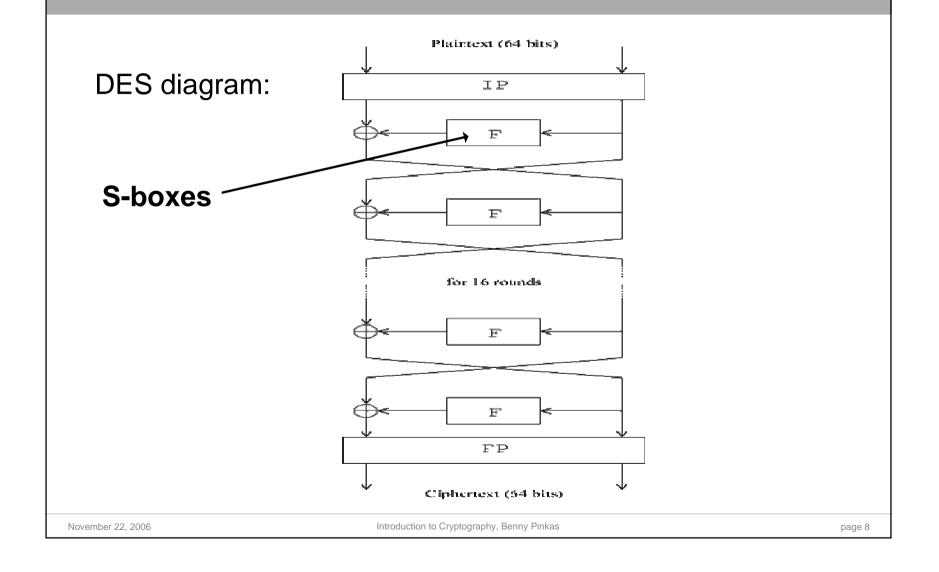


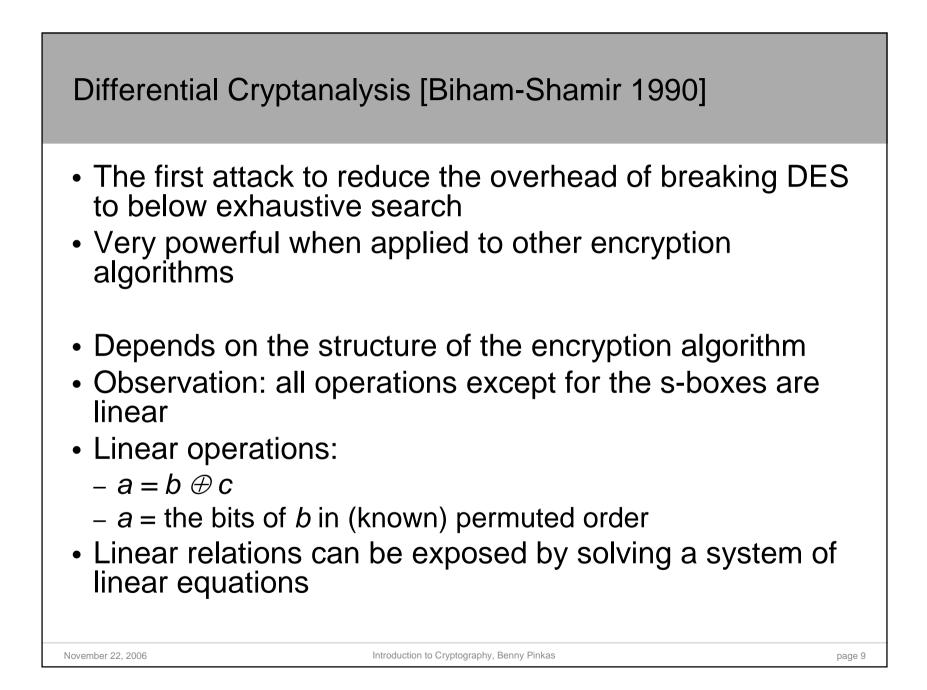
- Very careful design (it is now clear that random choices for the S-boxes result in weak encryption).
- Each s-box maps 6 bits to 4 bits:
  - A 4×16 table of 4-bit entries.
  - Bits 1 and 6 choose the row, and bits 2-5 choose column.
  - Each row is a *permutation* of the values 0,1,...,15.
    - Therefore, given an output there are exactly 4 options for the input
  - Changing one input bit changes at least two output bits  $\Rightarrow$  avalanche effect.

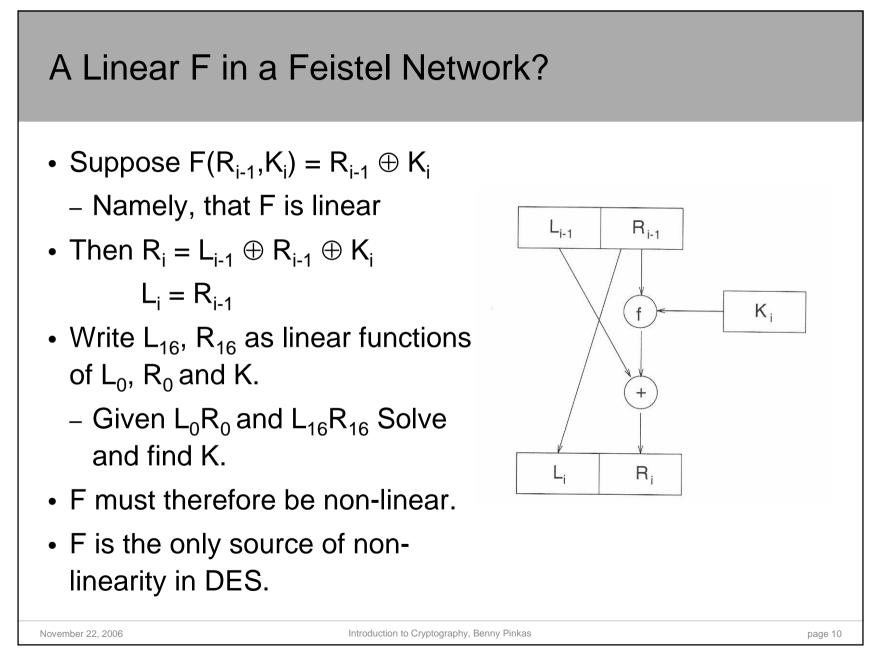
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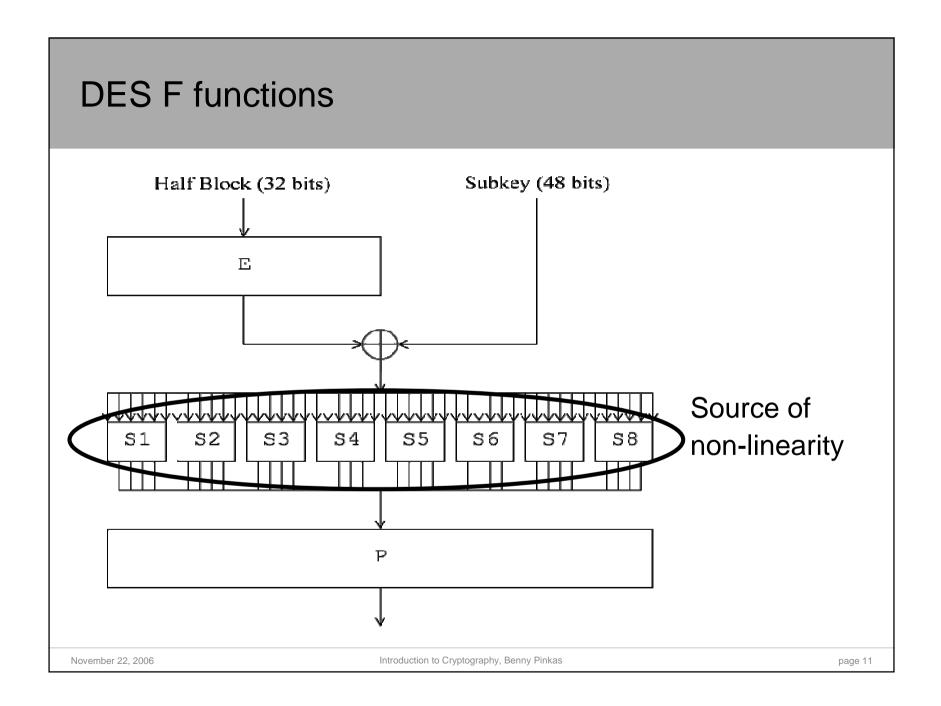
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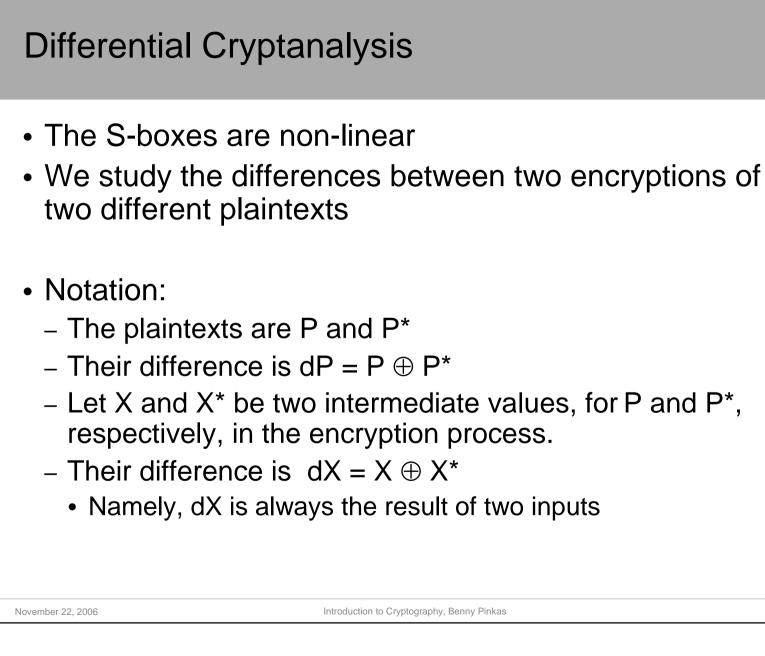
### Differential Cryptanalysis of DES

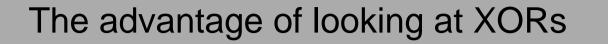










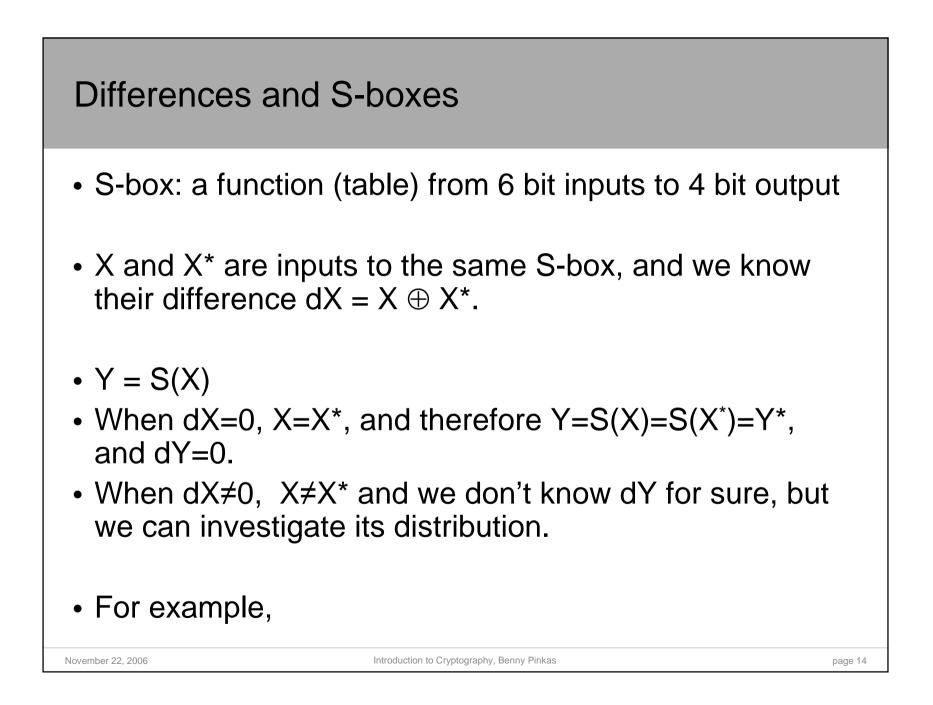


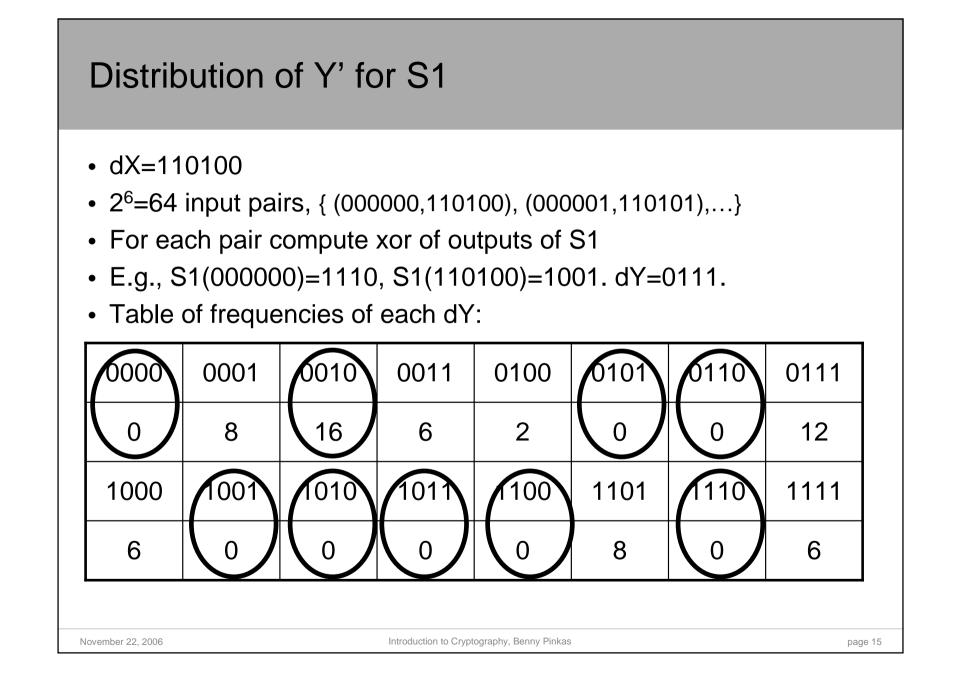
- It's easy to predict the difference of the results of linear operations
- Unary operations, (e.g. P is a permutation of the order of the bits of X)

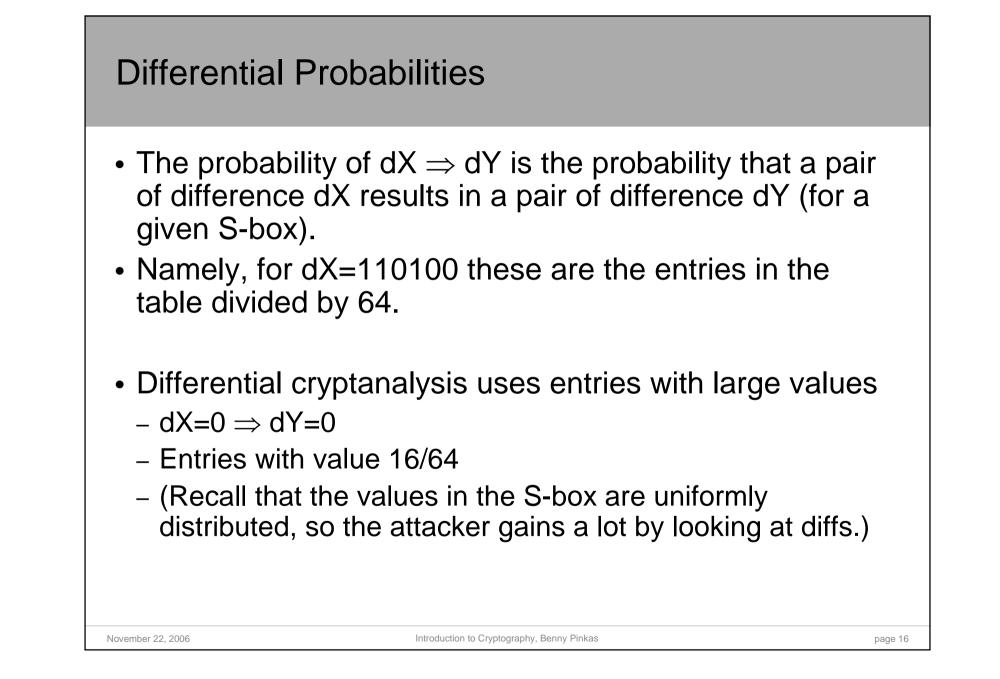
$$- dP(x) = P(x) \oplus P(x^*) = P(x \oplus x^*) = P(dx)$$

- XOR
  - $\begin{array}{ll} -d(x\oplus y)=(x\oplus y)\oplus (x^{*}\oplus y^{*})=(x\oplus x^{*})\oplus (y\oplus y^{*}) & = \\ dx\oplus dy & \end{array}$
- Mixing the key
  - $d(x \oplus k) = (x \oplus k) \oplus (x^* \oplus k) = x \oplus x^* = dx$
  - The result here is key independent (the key disappears)



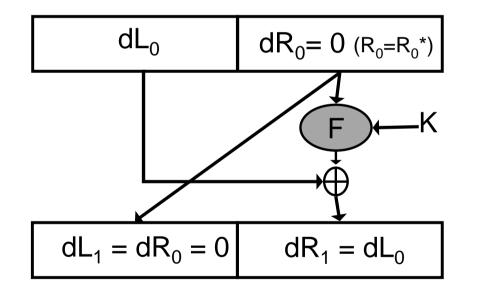








Inputs:  $L_0R_0$ ,  $L_0^*R_0^*$ , s.t.  $R_0=R_0^*$ . Namely, inputs whose xor is  $dL_0 0$ 

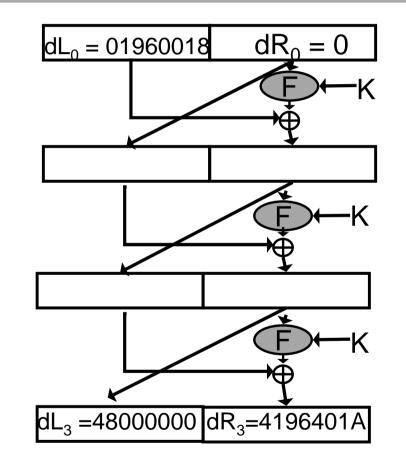


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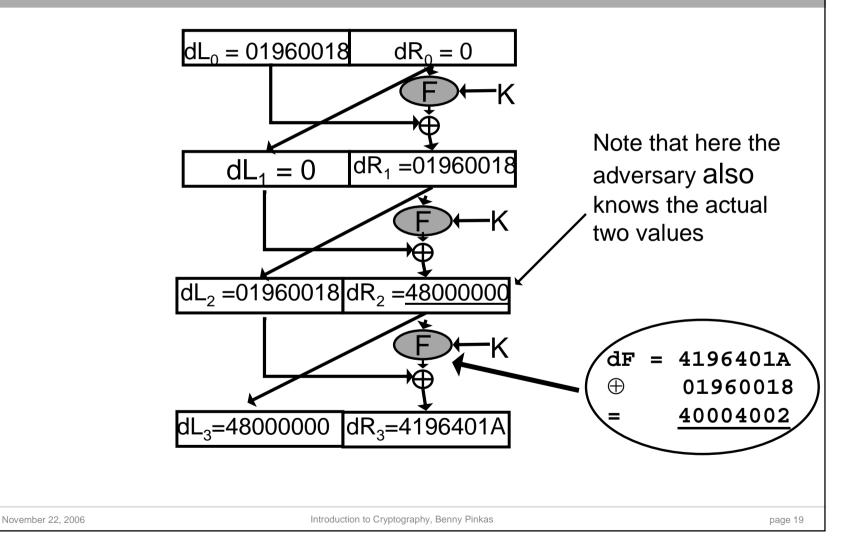
### 3 Round DES

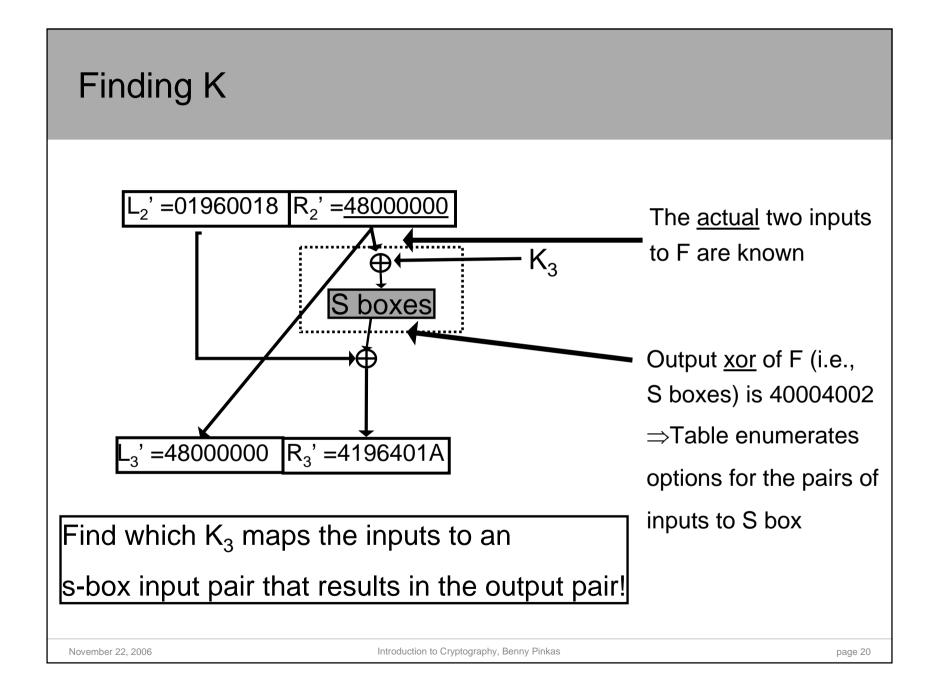


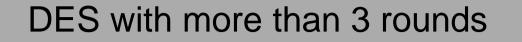
The attacker knows the two plaintext/ciphertext pairs, and therefore also their differences

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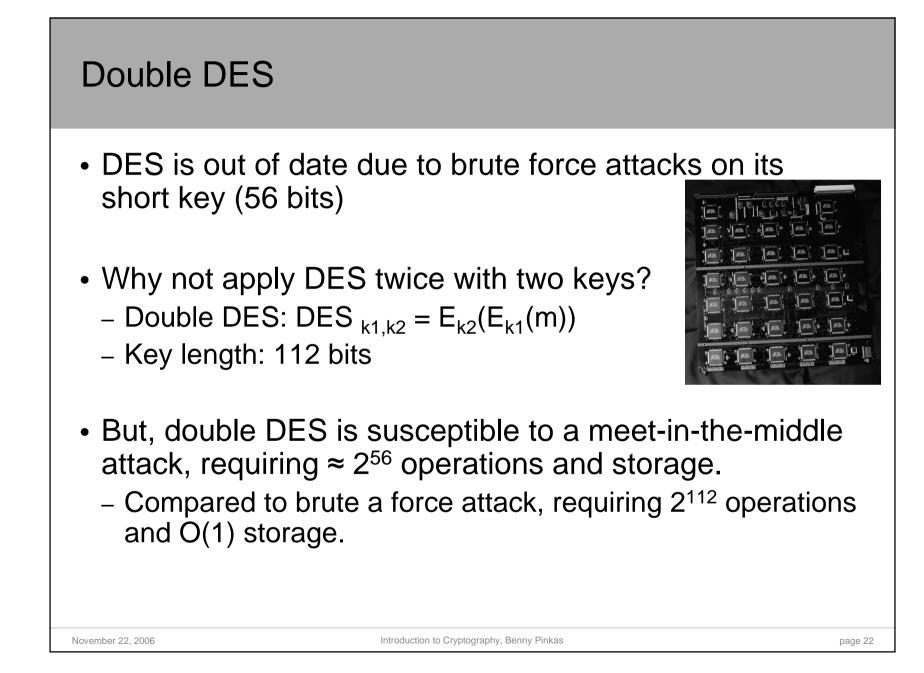
Intermediate differences equal to plaintext/ciphertext differences







- Carefully choose pairs of plaintexts with specific xor, and determine xor of pairs of intermediate values at various rounds.
- E.g., if dL<sub>0</sub>=40080000<sub>x</sub>, dR<sub>0</sub>=04000000<sub>x</sub>
  Then, with probability ¼, dL<sub>3</sub>=04000000<sub>x</sub>, dR<sub>3</sub>=4008000<sub>x</sub>
- 8 round DES is broken given 2<sup>14</sup> chosen plaintexts.
- 16 round DES is broken given 2<sup>47</sup> chosen plaintexts...



# Meet-in-the-middle attack

• Meet-in-the-middle attack

$$- c = E_{k2}(E_{k1}(m)) - D_{k2}(c) = E_{k1}(m)$$

- The attack:
  - Input: (*m*,*c*) for which  $c = E_{k2}(E_{k1}(m))$
  - For every possible value of  $k_1$ , generate and store  $E_{k1}(m)$ .
  - For every possible value of  $k_2$ , generate and store  $D_{k2}(c)$ .
  - Match  $k_1$  and  $k_2$  for which  $E_{k1}(m) = D_{k2}(c)$ .
  - Might obtain several options for  $(k_1,k_2)$ . Check them or repeat the process again with a new (m,c) pair (see next slide)
- The attack is applicable to any iterated cipher. Running time and memory are O(2<sup>|k|</sup>), where |k| is the key size.

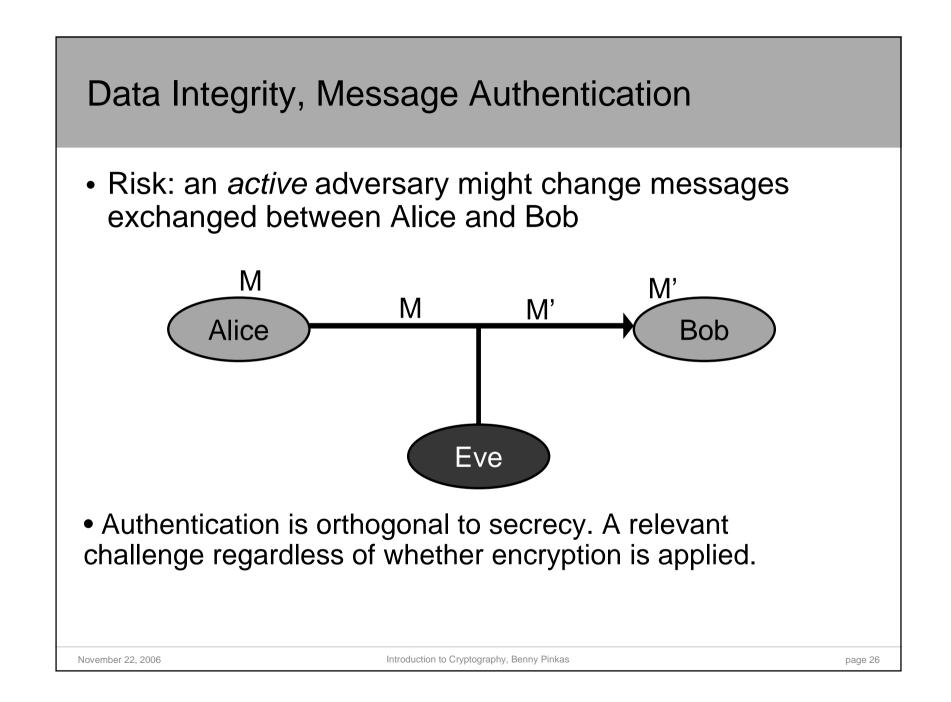
Meet-in-the-middle attack: how many pairs to check?

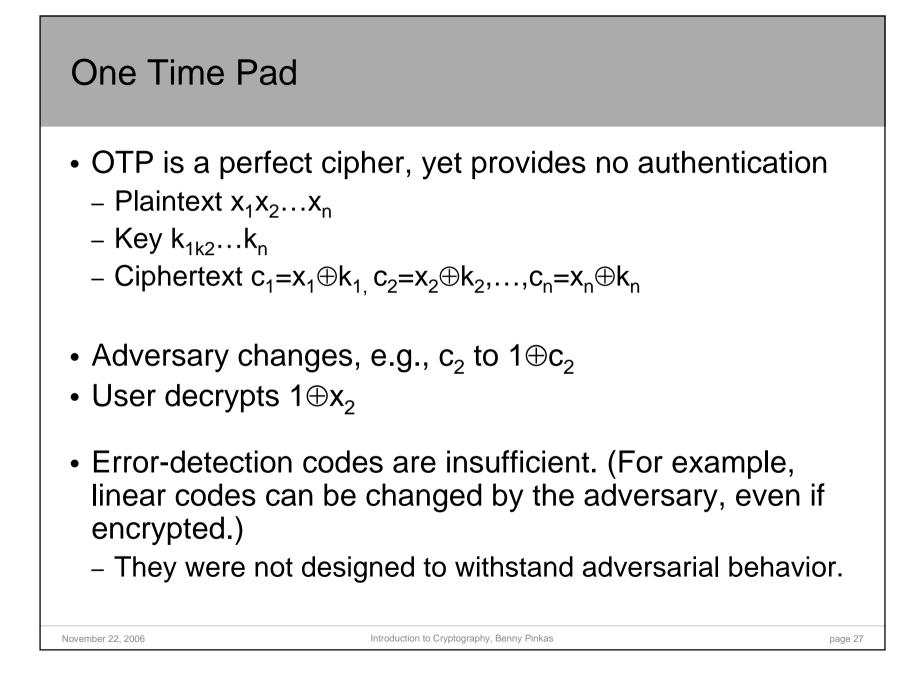
- The plaintext and the ciphertext are 64 bits long
- The key is 56 bits long
- Suppose that we are given one plaintext-ciphertext pair (m,c)
  - The attack looks for k1,k2, such that  $D_{k2}(c) = E_{k1}(m)$
  - The correct values of k1,k2 satisfies this equality
  - There are  $2^{112}$  (actually  $2^{112}$ -1) other values for  $k_1, k_2$ .
  - Each one of these satisfies the equalities with probability 2-64
  - We therefore expect to have  $2^{112-64}=2^{48}$  candidates for  $k_1, k_2$ .
- Suppose that we are given one pairs (m,c), (m',c')
  - The correct values of k1,k2 satisfies both equalities
  - There are  $2^{112}$  (actually  $2^{112}$ -1) other values for  $k_1, k_2$ .
  - Each one of these satisfies the equalities with probability 2<sup>-128</sup>
  - We therefore expect to have  $2^{112-128} < 1$  false candidates for  $k_1, k_2$ .

### **Triple DES**

- 3DES  $_{k1,k2} = E_{k1}(D_{k2}(E_{k1}(m)))$
- Why use Enc(Dec(Enc())) ?
  - Backward compatibility: setting  $k_1 {=} k_2$  is compatible with single key DES
- Only two keys
  - Effective key length is 112 bits
  - Why not use three keys? There is a meet-in-the-middle attack with 2<sup>112</sup> operations
- 3DES provides good security. Widely used. Less efficient.

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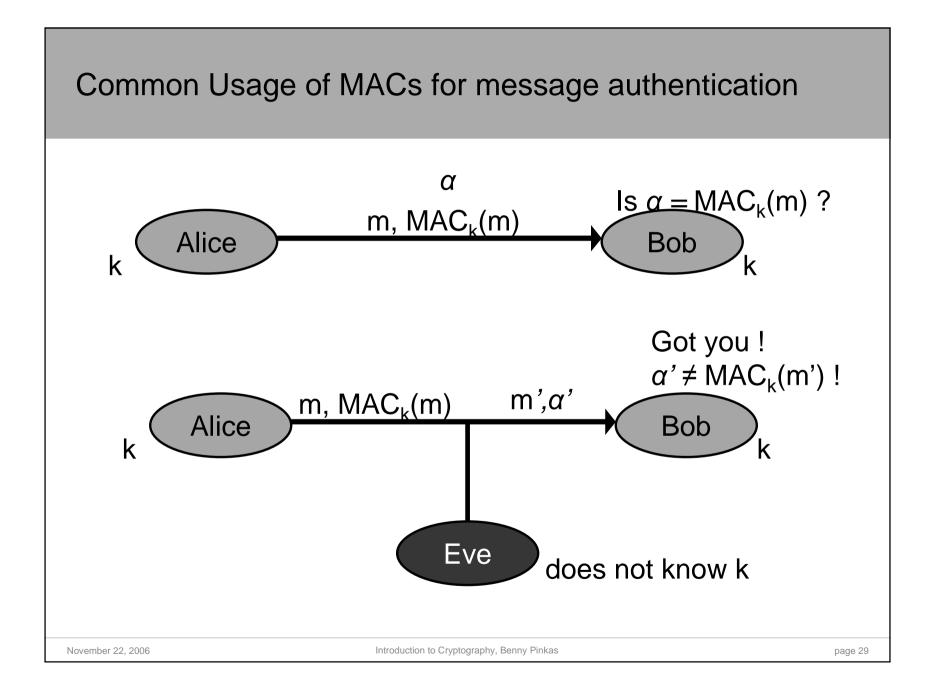




### Definitions

- Scenario: Alice and Bob share a secret key K.
- Authentication algorithm:
  - Compute a Message Authentication Code:  $\alpha = MAC_{\kappa}(m)$ .
  - Send m and  $\alpha$
- Verification algorithm:  $V_{\kappa}(m, \alpha)$ .
  - $V_{\kappa}(m, MAC_{\kappa}(m)) = accept.$
  - For  $\alpha \neq MAC_{\kappa}(m)$ ,  $V_{\kappa}(m, \alpha) = reject$ .
- How does  $V_k(m)$  work?
  - Receiver knows k. Receives m and  $\alpha$ .
  - Receiver uses k to compute  $MAC_{\kappa}(m)$ .

- 
$$V_{\kappa}(m, \alpha) = 1$$
 iff  $MAC_{\kappa}(m) = \alpha$ .



#### Requirements

- Security: The adversary,
  - Knows the MAC algorithm (but not *K*).
  - Is given many pairs  $(m_i, MAC_{\kappa}(m_i))$ , where the  $m_i$  values might also be chosen by the adversary (chosen plaintext).
  - Cannot compute (*m*,  $MAC_{\kappa}(m)$ ) for any new *m* ( $\forall i \ m \neq m_i$ ).
  - The adversary must not be able to compute  $MAC_{K}(m)$ even for a message m which is "meaningless" (since we don't know the context of the attack).
- Efficiency: output must be of fixed length, and as short as possible.
  - $\Rightarrow$  The MAC function is not 1-to-1.
  - $\Rightarrow$  An n bit MAC can be broken with prob. of at least 2<sup>-n</sup>.

